

# Increase the power absorbtion efficiency in superconducting waveguides

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We increase the power absorption efficiency for TE<sub>0</sub> and TM<sub>0</sub> modes in superconducting traveling wave photo detectors and compensate a large part of the lost power in the substrate SiO<sub>2</sub> layer of a waveguide with an active superconducting YBCO layer, by using an optimized supplementary YSZ layer thickness.

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## 1. Introduction

The knowledge of optical propagation characteristics of the superconducting optical waveguides is important for the project of a new class of ultra sensitive, ultra fast and ultra slow noise detectors based on a distributed photo detection scheme of traveling wave devices [1]. The key phenomenon for the detection of light for frequencies above the gap frequency of superconductors is to annihilate Cooper pairs and create two times as many normal electrons as the broken Cooper pairs [1].

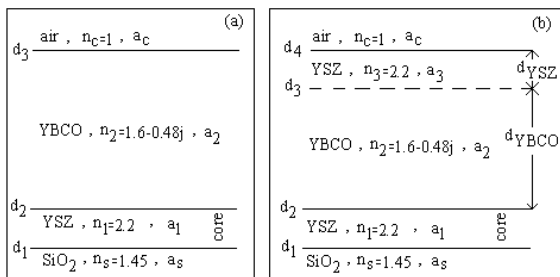


Fig. 1. (a) Schematic of a conventional superconductor planar waveguide,  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ; (b) schematic of a superconductor planar waveguide with a supplementary YSZ layer,  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_{\text{YBCO}} + d_{\text{YSZ}} = 0.2\mu\text{m}$ .

The analyzed single mode waveguide [2] (Fig.1a) consists of a lossy superconductor (YBCO) layer placed on a dielectric [yttria stabilized zirconia (YSZ)] surface and this structure is enclosed by air above and a semi-infinite dielectric (SiO<sub>2</sub>) layer below. Because YSZ dielectric core layer between the SiO<sub>2</sub> substrate and superconducting layer is very thin, modes TE<sub>0</sub> and TM<sub>0</sub> are not tightly confined but extend quite far from the core layer of the waveguide.

Thus, a large portion of optical power is absorbed by the YBCO layer and contributes to the photo detection process and unfortunately another great portion of power

is absorbed by the substrate layer which does not contribute to the light detection.

In this paper, we introduce an improved structure (Fig.1b) which includes an optimized supplementary YSZ layer thickness sandwiched between YBCO and air layers. In this single mode structure, a larger portion of optical power, for TE<sub>0</sub> and TM<sub>0</sub> evanescent modes, is absorbed by the YBCO layer and contributes to the performance of the light detector.

## 2. Superconducting optical planar waveguide

The scalar-wave equation for a slab waveguide is given by

$$\frac{d^2\psi(y)}{dy^2} + k^2 n^2(y)\psi(y) = \beta^2\psi(y), \quad (1)$$

where  $\beta$  is the propagation constant,  $k$  is the free space wave number,  $n(y)$  is the refractive index profile

$$n(y) = \begin{cases} n_s, & \text{for } y < d_1 = 0, \\ n_i, & \text{for } d_i < y < d_{i+1}, i = 1, 2, \\ n_c, & \text{for } d_3 < y, \end{cases} \quad (2)$$

$$n(y) = \begin{cases} n_s, & \text{for } y < d_1 = 0, \\ n_i, & \text{for } d_i < y < d_{i+1}, i = 1, 2, 3, \\ n_c, & \text{for } d_4 < y, \end{cases} \quad (2')$$

$n_s$ ,  $n_1$ ,  $n_2$ ,  $n_3$ , and  $n_c$  are the refractive index of the SiO<sub>2</sub> substrate, YSZ film core, YBCO film, YSZ additional film and air cladding, respectively. The effective index  $\beta/k$  for the TE and TM modes can be found from the dispersion equation which is obtained by applying the boundary conditions at the interfaces between different layers.

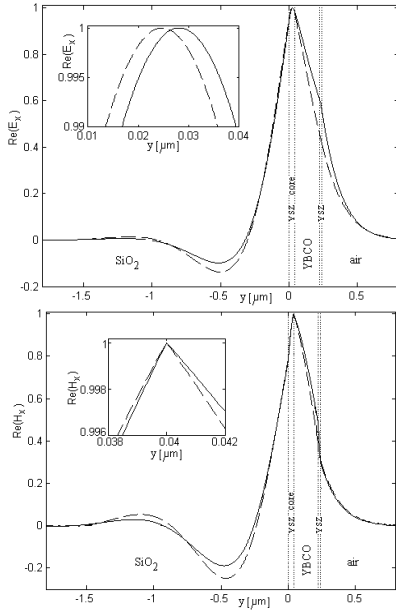


Fig. 2. The real part of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for a waveguide (Fig.1a, - -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ,  $d_{\text{YSZ}} = 0\mu\text{m}$ ,  $n_s = 1.45$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$  and for a waveguide (Fig.1b, -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.22\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.18\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.02\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ , respectively. The inset is a detail of maxima for  $E_x$  and  $H_x$ .

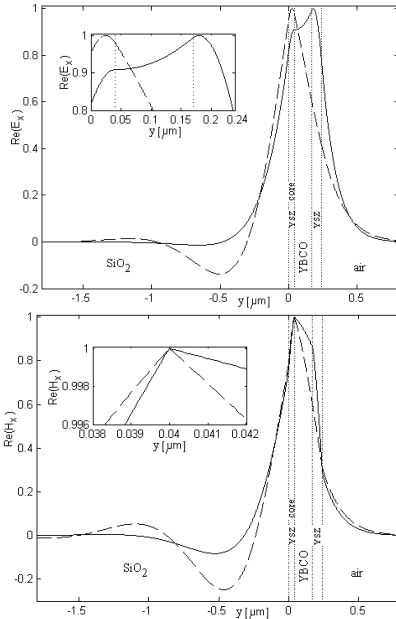


Fig. 3. The real part of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for a waveguide (Fig.1a, - -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ,  $d_{\text{YSZ}} = 0\mu\text{m}$ ,  $n_s = 1.45$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$  and for a waveguide (Fig.1b, -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.17\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ , respectively. The inset is a detail of maxima for  $E_x$  and  $H_x$ .

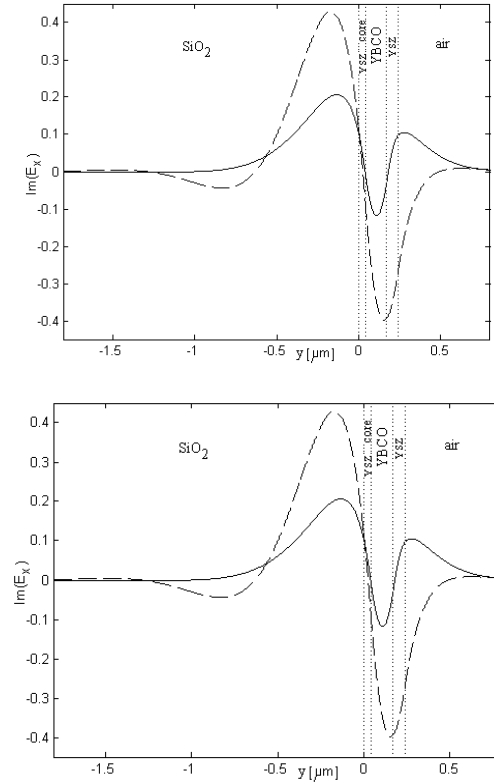


Fig. 4. The imaginary part of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for a waveguide (Fig.1a, - -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ,  $d_{\text{YSZ}} = 0\mu\text{m}$ ,  $n_s = 1.45$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$  and for a waveguide (Fig.1b, -) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.17\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ , respectively. The inset is a detail of maxima for  $E_x$  and  $H_x$ .

The variational exact solution [3] of the scalar wave Eq. (1) is found from the functional

$$J_{11} = \int_{-\infty}^{d_1} \left[ -\frac{f_s'^2}{n_s^2 \xi} + (kn_s^{1-\xi} f_s)^2 \right] dy \quad (3)$$

$$+ \sum_{i=1}^2 \int_{d_i}^{d_{i+1}} \left[ -\frac{f_i'^2}{n_i^2 \xi} + (kn_i^{1-\xi} f_i)^2 \right] dy + \int_{d_3}^{\infty} \left[ -\frac{f_c'^2}{n_c^2 \xi} + (kn_c^{1-\xi} f_c)^2 \right] dy,$$

$$J_{11} = \int_{-\infty}^{d_1} \left[ -\frac{f_s'^2}{n_s^2 \xi} + (kn_s^{1-\xi} f_s)^2 \right] dy \quad (3')$$

$$+ \sum_{i=1}^3 \int_{d_i}^{d_{i+1}} \left[ -\frac{f_i'^2}{n_i^2 \xi} + (kn_i^{1-\xi} f_i)^2 \right] dy + \int_{d_4}^{\infty} \left[ -\frac{f_c'^2}{n_c^2 \xi} + (kn_c^{1-\xi} f_c)^2 \right] dy,$$

subject to the constraint that

$$I_{11} = \int_{-\infty}^{d_1} \frac{f_s^2}{2\xi} dy + \sum_{i=1}^2 \int_{d_i}^{d_{i+1}} \frac{f_i^2}{n_i^2 \xi} dy + \int_{d_3}^{\infty} \frac{f_c^2}{n_c^2 \xi} dy, \quad (4)$$

$$I_{11} = \int_{-\infty}^{d_1} \frac{f_s^2}{n_s^{2\xi}} dy + \sum_{i=1}^3 \int_{d_i}^{d_{i+1}} \frac{f_i^2}{n_i^{2\xi}} dy + \int_{d_4}^{\infty} \frac{f_c^2}{n_c^{2\xi}} dy, \quad (4')$$

$$\beta^2 = \frac{J_{11}}{I_{11}} \quad (5)$$

where  $\xi$  reads as 0 for TE polarized waves and 1 for TM polarized waves and the exact functions  $f_s$ ,  $f_i$  and  $f_c$  are given by

$$f_s(y) = A_s \exp(a_s y), \quad y < d_1, \quad (6)$$

$$f_s(y) = A_s \exp(a_s y), \quad y < d_1, \quad (6')$$

$$f_i(y) = A_i \cos[a_i(y-d_i)] + B_i \sin[a_i(y-d_i)], \quad d_i < y < d_{i+1}, i=1,2 \quad (7)$$

$$f_i(y) = A_i \cos[a_i(y-d_i)] + B_i \sin[a_i(y-d_i)], \quad d_i < y < d_{i+1}, i=1,2,3 \quad (7')$$

$$f_c(y) = A_c \exp(-a_c(y-d_3)), \quad y > d_3, \quad (8)$$

$$f_c(y) = A_c \exp(-a_c(y-d_4)), \quad y > d_4, \quad (8')$$

And

$$a_s = \sqrt{\beta^2 - (n_s k)^2}, \quad a_c = \sqrt{\beta^2 - (n_c k)^2}, \quad (9)$$

$$a_i = \sqrt{(n_i k)^2 - \beta^2}, \quad i=1,2,$$

$$a_s = \sqrt{\beta^2 - (n_s k)^2}, \quad a_c = \sqrt{\beta^2 - (n_c k)^2}, \quad (9')$$

$$a_i = \sqrt{(n_i k)^2 - \beta^2}, \quad i=1,2,3,$$

$$A_1 = A_s = 1, B_1 = \frac{n_1^{2\xi}}{n_s^{2\xi}} \frac{a_s}{a_1}, \quad (10)$$

$$A_1 = A_s = 1, B_1 = \frac{n_1^{2\xi}}{n_s^{2\xi}} \frac{a_s}{a_1}, \quad (10')$$

$$A_i = A_{i-1} \cos[a_{i-1}(d_i - d_{i-1})] + B_{i-1} \sin[a_{i-1}(d_i - d_{i-1})], \quad i=1,2, \quad (11)$$

$$A_i = A_{i-1} \cos[a_{i-1}(d_i - d_{i-1})] + B_{i-1} \sin[a_{i-1}(d_i - d_{i-1})], \quad i=1,2,3, \quad (11')$$

$$B_i = \frac{n_i^{2\xi}}{n_{i-1}^{2\xi}} \frac{a_{i-1}}{a_i} (B_{i-1} \cos[a_{i-1}(d_i - d_{i-1})] - A_{i-1} \sin[a_{i-1}(d_i - d_{i-1})]), \quad i=1,2, \quad (12)$$

$$B_i = \frac{n_i^{2\xi}}{n_{i-1}^{2\xi}} \frac{a_{i-1}}{a_i} (B_{i-1} \cos[a_{i-1}(d_i - d_{i-1})] - A_{i-1} \sin[a_{i-1}(d_i - d_{i-1})]), \quad i=1,2,3, \quad (12')$$

$$A_c = A_2 \cos[a_2(d_3 - d_2)] + B_2 \sin[a_2(d_3 - d_2)], \quad (13)$$

$$A_c = A_3 \cos[a_3(d_4 - d_3)] + B_3 \sin[a_3(d_4 - d_3)], \quad (13')$$

The relations (2 - 13) and (2' - 13') correspond to Fig. 1 (a) and (b), respectively.

The solutions of the dispersion equation (5) give the propagation constants  $\beta$  and the effective index  $\beta/k$  of the waveguide. There are numerous methods available to solve the dispersion equation [2-5].

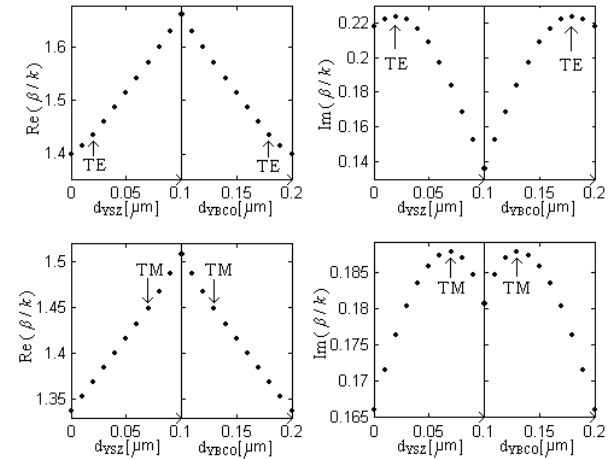


Fig. 5. Real and imaginary parts of the effective index  $\beta/k$ , versus a supplementary YSZ layer thickness  $d_{YSZ}$ , for  $TE_0$  and  $TM_0$  modes.  $\text{Re}(\beta/k)$  and  $\text{Im}(\beta/k)$  as a function of the YBCO thickness  $d_{YBCO}$ .

The total power carried by the TE (TM) mode is related to the electric (magnetic) field through the relation [6-7]:

$$P = \frac{1}{2\omega\mu_0^{1-\xi}\varepsilon_0^\xi} \int_{-\infty}^{\infty} \text{Re} \left[ \beta \frac{|\psi(y)|^2}{n^{2\xi}(y)} \right] dy, \quad (14)$$

where  $\xi$  reads as 0 for TE ( $\psi = E_x$ ) polarized waves and 1 for TM ( $\psi = H_x$ ) polarized waves,  $\mu_0$  is the magnetic permeability of free space,  $\varepsilon_0$  is the permittivity in a vacuum and  $\omega$  is the angular frequency. The effect of YSZ additional thickness on the confinement of the light in different parts of the waveguide structure is related to

the fractional power  $P_i/P$ , where  $P_i$  is the power carried by a mode in a specific part of the waveguide.

### 3. Numerical results and conclusions

We have calculated the exact value of the effective index  $\beta/k$  for the guided modes in a waveguide (Fig.1 (a) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ,  $d_{\text{YSZ}} = 0\mu\text{m}$ ,  $n_s = 1.45$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$  [8],  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ ,  $\beta_0/k = 1.396050-0.217941j$  for  $\text{TE}_0$  and  $\beta_0/k = 1.337123-0.166104j$  for  $\text{TM}_0$ ) and for a waveguide (Fig.1 (b) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.22\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.18\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.02\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ ,  $\beta_0/k = 1.434481-0.223274j$  for  $\text{TE}_0$  and  $\beta_0/k = 1.368876-0.176286j$  for  $\text{TM}_0$ ) with an additional YSZ layer but with  $d_{\text{YBCO}} + d_{\text{YSZ}} = 0.2\mu\text{m}$ .

Fig. 2 shows the real parts of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for these waveguides. The field amplitude has been normalized to a maximum value of unity. Also, we have calculated the exact value of the effective index  $\beta/k$  for a waveguide (Fig.1 (b) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.17\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ ,  $\beta_0/k = 1.571623-0.183812j$  for  $\text{TE}_0$  and  $\beta_0/k = 1.448892-0.187739j$  for  $\text{TM}_0$ ) with an additional YSZ layer but with  $d_{\text{YBCO}} + d_{\text{YSZ}} = 0.2\mu\text{m}$ .

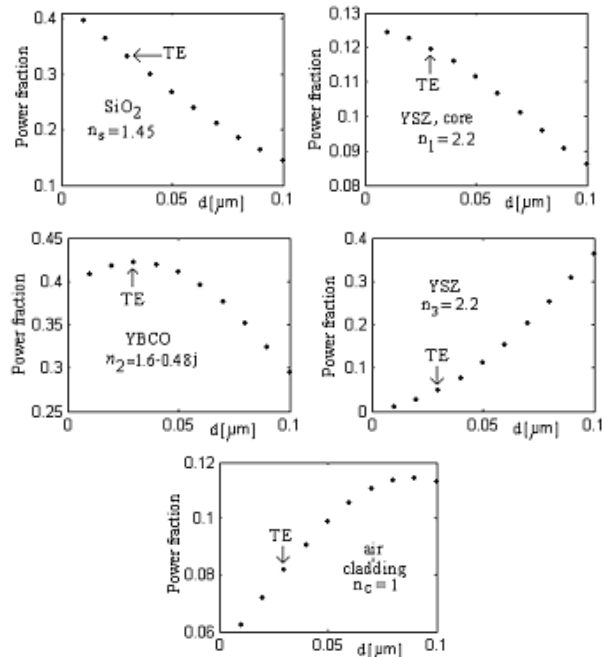


Fig. 6. Fraction of the power versus a supplementary YSZ layer thickness  $d = d_{\text{YSZ}}$ , carried by the fundamental mode  $\text{TE}_0$  in different parts of the waveguide structure.

Fig. 3 shows the real parts of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for this waveguide in comparison with the waveguide from Fig. 1 (a). Fig. 4 shows the imaginary part of the fundamental field profiles ( $E_x$ ,  $H_x$ ) for a waveguide

(Fig. 1 (a)) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.2\mu\text{m}$ ,  $d_{\text{YSZ}} = 0\mu\text{m}$ ,  $n_s = 1.45$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$  and for a waveguide (Fig. 1 (b)) with  $d_1 = 0\mu\text{m}$ ,  $d_2 = d_{\text{YSZcore}} = 0.04\mu\text{m}$ ,  $d_3 = 0.17\mu\text{m}$ ,  $d_4 = 0.24\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ,  $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $n_s = 1$ ,  $n_1 = 2.2$ ,  $n_2 = 1.6-0.48j$ ,  $n_3 = 2.2$ ,  $n_c = 1$ ,  $\lambda = 0.85\mu\text{m}$ , respectively.

Figs. 2 – 3 show that by increasing the thickness of the additional YSZ layer and decreasing the thickness of the active YBCO layer ( $d_{\text{YBCO}} + d_{\text{YSZ}} = 0.2\mu\text{m}$ ) the maximum of the fundamental mode  $E_x$  is shifted towards the YBCO layer, but the maximum for the fundamental mode  $H_x$  remains to a constant value  $y = 0.04\mu\text{m}$ .

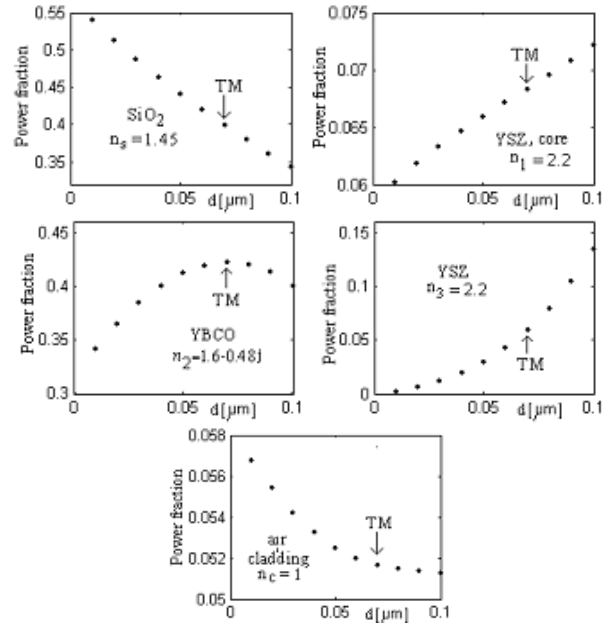


Fig. 7. Fraction of the power versus a supplementary YSZ layer thickness  $d = d_{\text{YSZ}}$ , carried by the fundamental mode  $\text{TM}_0$  in different parts of the waveguide structure.

Fig. 5 shows the effect of thickening the supplementary YSZ layer on the real and imaginary parts of the effective index for  $\text{TE}_0$  and  $\text{TM}_0$  modes. If the thickness of the additional YSZ layer is increased, the real part of the effective index is also increased. The imaginary part of the effective index shows a maximum at small values of the additional YSZ thickness ( $d_{\text{YSZ}} = 0.02\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.18\mu\text{m}$ ) for  $\text{TE}_0$  mode and at high values of the additional YSZ thickness ( $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ) for  $\text{TM}_0$  mode. The maximum for the imaginary part of the effective index for  $\text{TM}_0$  mode is smaller and shifted to higher values of the supplementary YSZ thickness in comparison with the  $\text{TE}_0$  mode.

Figs. 6-7 show the fraction of the power, versus a supplementary YSZ layer thickness  $d = d_{\text{YSZ}}$ , carried by the  $\text{TE}_0$  and  $\text{TM}_0$  modes (per unit length in  $x$  direction) along the  $z$  axis, for different parts of the waveguide structure. With an increase in the additional YSZ layer thickness, the fraction of the power in the  $\text{SiO}_2$  substrate is

diminished and the power is increased in active YBCO layer. The fraction of the power guided in active YBCO layers shows a maximum at small values of the supplementary YSZ layer thickness ( $d_{\text{YSZ}} = 0.03\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.17\mu\text{m}$ ) for  $\text{TE}_0$  mode and at high values (the same as in Fig.5) of the additional YSZ layer thickness ( $d_{\text{YSZ}} = 0.07\mu\text{m}$ ,  $d_{\text{YBCO}} = 0.13\mu\text{m}$ ) for  $\text{TM}_0$  mode. The maximum of the fractional power guided in superconducting layers for  $\text{TM}_0$  mode is very close (0.42) and shifted to higher values of the additional YSZ thickness in comparison with the  $\text{TE}_0$  mode.

Thus, although the active YBCO layer thickness was decreased, the power absorption efficiency for  $\text{TE}_0$  and  $\text{TM}_0$  modes in this layer is increased by using an optimized supplementary YSZ layer thickness by decreasing the lost power in the substrate  $\text{SiO}_2$  layer of a waveguide.

Our analyses are important for engineering project of multilayer waveguides with layers consists of dielectric and superconducting materials.

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