

Calculation of the crystal field parameters of the $\text{ZnAl}_2\text{O}_4:\text{Eu}^{3+}$

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Zinc aluminate (ZnAl_2O_4) doped with rare earth metal ions has been investigated most frequently because of the unique luminescent properties resulting from its stability and high emission quantum yields. The present work is devoted to the calculation of the crystal field parameters and the energy levels of the trivalent europium doped in ZnAl_2O_4 spinel, using a theoretical model of the crystal field. The obtained results are compared with the experimental data and discussed.

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1. Introduction

The zinc aluminate spinel (ZnAl_2O_4) offers many advantages, such as high thermal and chemical stability, hydrophobic behavior, high mechanical resistance, low sintering temperature, and high quantum yields [1-4].

The structure of the zinc aluminate spinel ZnAl_2O_4 is presented in the Fig. 1.

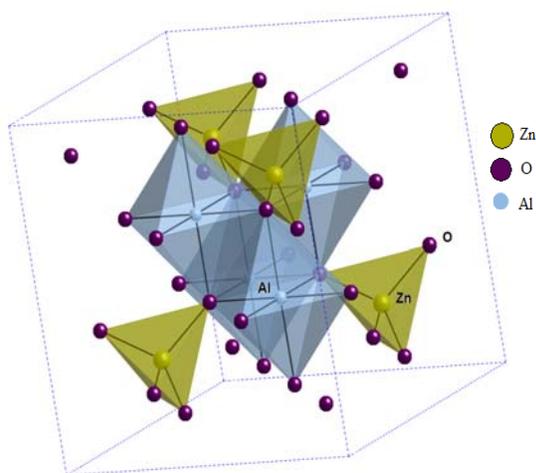


Fig. 1. The structure of ZnAl_2O_4 .

Zinc aluminate doped with rare earth metal ions has been investigated most frequently because of the unique luminescent properties resulting from its stability and high emission quantum yields. Recently, rare earth metal ions activated ZnAl_2O_4 phosphors have been studied thanks to the unique luminescent properties resulting from its stability and high emission quantum yields [1, 2 and 4].

Aluminum-based spinel denotes an interesting sort of oxide ceramics with significant technological applications.

Of these, gahnite (ZnAl_2O_4) is a useful semiconductor (3.8 eV), and thus it can be used as transparent conductor, dielectric material, and optical material [5].

The normal spinel ZnAl_2O_4 belongs to the orthorhombic $Fd3m$ space group with the unit cell parameters $a = b = c = 8.0875 \text{ \AA}$ [6].

The Eu^{3+} ion will substitute the Al^{3+} ion in an octahedral site in the ZnAl_2O_4 spinel, without charge compensation. Despite the existence of the experimental data concerning the $\text{Eu}^{3+}:\text{ZnAl}_2\text{O}_4$ system, the explanation of the theoretical scheme of the energy levels is absent.

The present work is devoted to the modeling the crystal field parameters of the $\text{Eu}^{3+}:\text{ZnAl}_2\text{O}_4$ system in the superposition model of the crystal field and simulation the low-lying energy levels of the trivalent europium doped in ZnAl_2O_4 spinel, by diagonalization the Hamiltonian of the system. The obtained results are compared with experimental data and discussed.

2. Modeling of the crystal field parameters

In the normal ZnAl_2O_4 spinel structure, the zinc and aluminium cations locate at tetrahedrally and octahedrally coordinated A and B sites with local site symmetry T_d and D_{3d} [6]. Zinc atoms locate on the A- sites are surrounded by four oxygen atoms, whereas aluminium cation at the B- sites, surrounded by six oxygen atoms.

Eu^{3+} ions are expected to occupy Al^{3+} sites in the octahedral symmetry and this substitution does not require charge compensation. These ions have different ionic radii: $r_{\text{Eu}^{3+}} = 0.95 \text{ \AA}$ and $r_{\text{Al}^{3+}} = 0.54 \text{ \AA}$, and as result the site symmetry of the trivalent europium doped in ZnAl_2O_4 will decrease from octahedral to low (close to D_{3d}) symmetry.

In order to describe the energy levels of the ground state of rare-earth ions doped in crystals, we use the Hamiltonian [7]:

$$H = \sum B_k^q O_k^q \quad (1)$$

where:

B_k^q - are the crystal field parameters (CFP) associated with the extended Stevens operators O_k^q .

The crystal field parameters will be calculate using the superposition model. In this model the crystal field parameters may be expressed as [8-10]:

$$B_k^q = \sum_L \bar{B}_k(R_L) K_k^q(\theta_L, \phi_L) \quad (2)$$

where:

K_k^q - are the coordination factors [8-10] defined in terms of the angles θ_L and ϕ_L of the L ligand positions.

The $\bar{B}_k(R_L)$ are the intrinsic parameters and they are given by [8-10]:

$$\bar{B}_k(R_L) = \bar{B}_k(R_0) \left(\frac{R_0}{R_L} \right)^{t_k} \quad (3)$$

Here the $\bar{B}_k(R_0)$ are the intrinsic crystal field parameters corresponding to R_0 reference distance; R_L is the distance from impurity ion to ligand L and R_0 represents the reference distance; t_k are the power law exponents that are adjustable semi-empirical parameters [8-10].

The intrinsic crystal field parameters $\bar{B}_k(R_0)$ can be transferred from similar cluster [EuO₆]⁹⁻ [7]. R_L can be approximate as [11]:

$$R_L \approx R_h + \frac{1}{2}(r_L - r_h) \quad (4)$$

where:

R_h is the distance between Al³⁺ and ligands, and $r_L(\text{Eu}^{3+}) = 0.95\text{\AA}$; $r_h(\text{Al}^{3+}) = 0.54\text{\AA}$.

Using the geometry of the host matrix [6], the values of the intrinsic parameters $\bar{B}_k(R_0)$ for Eu³⁺- O²⁻ can be transferred from [12-14]. For the adjustable parameters t_k we taken the values $t_2 = 5$, $t_4 = 9$ and $t_6 = 13$, given by the point charge model of crystal field theory. Thus, the crystal field parameters B_k^q from (1) are calculated, using the Eqs. ((2), (3)).

3. Results and discussion

In the Table 1 are given the reference distance (R_0) and crystal field intrinsic parameters at reference distance.

Table 1. The intrinsic parameters.

$R(\text{\AA})$	$R_0(\text{\AA})$	$\bar{B}_2(\text{cm}^{-1})$	$\bar{B}_4(\text{cm}^{-1})$	$\bar{B}_6(\text{cm}^{-1})$
	[12]	[12-14]	[12-14]	[12-14]
2.50	2.98	370	35	21

In the Table 2 are given the crystal field parameters of Eu³⁺ doped in ZnAl₂O₄ calculated in the superposition model.

Table 2. The crystal field parameters.

Parameter	Superposition Model
B_2^0	743
B_4^0	-221
B_4^3	-4
B_6^0	-171
B_6^3	1
B_6^6	-1309

With these parameters and the parameters of free Eu³⁺ ions [15] we have diagonalized the Hamiltonian of the title system with SPECTRA, a computer program. The low-lying energy levels are presented in the Table 3.

Table 3. The energy levels of the Eu³⁺ doped in ZnAl₂O₄ spinel.

Energy levels	Experimental [17]	Calculate (this work)
7F_0	0	0
7F_1	381	372
7F_2	988	1090
7F_3	1987	1944
7F_4	3076	3098
7F_5	-	3920
7F_6	-	5465
5D_0	17301	19015
5D_1	18868	20128
5D_2	21598	22065
5D_3	24038	24478
5L_6	25253	25839

It can be seen from this table that the calculated values are close with experimental one [16], which confirm the validity of the superposition model of crystal field for this case. Also, we have given the position of two energy levels 7F_5 and 7F_6 which had not yet been observed experimentally.

4. Conclusions

In the present paper has been performed the crystal field calculation parameters and the low-lying energy levels for Eu^{3+} doped in ZnAl_2O_4 spinel.

The crystal field parameters of Eu^{3+} doped in ZnAl_2O_4 have been calculated in the frame of the superposition model of the crystal field. The low-lying energy level schemes of the europium ions in the studied host, has been calculated by diagonalizing the Hamiltonian of the system.

Reasonable agreement between the calculated and measured crystal field splittings confirms validity of the results obtained in this paper.

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